

IN THE CLAIMS

1.(currently amended) An extended Maxwell pair comprising:  
a pair of cylindrical gradient coils disposed coaxially around and along a z-axis extending in z-direction and symmetrically with respect to an origin, each being of radius a and of axial length d, said pair being mutually separated by a center-to-center distance  $z_0$  which is greater than d; and  
means for causing equal magnitude currents to flow through said gradient coils in mutually opposite directions;  
values of d and  $z_0$  being selected such that said equal currents generate a magnetic field along said z-axis with a linear gradient near said origin in said z-direction.  
a pair of cylindrical shield coils, said shield coils of equal radius and axially spaced and disposed coaxially around said gradient coils, each of said shield coils being of radius b which is greater than a, said means causing currents of equal magnitude and opposite sense and selected nonuniform axial current density dependence to flow through said shield coils, said shield coils causing [serving to cancel] cancellation of said gradient magnetic field outside said shield coils.

2. canceled

3. (original) The extended Maxwell pair of claim 1 wherein said magnetic field along said z-axis, when expanded in a polynomial form in z, does not include a cubic term.

4. canceled

5. (original) The extended Maxwell pair of claim 1 wherein each of said gradient coils comprises a helically rolled rectangular conductor sheet.

6. canceled

7. (previously amended) The extended Maxwell pair of claim 5 1 wherein each of said shield coils comprises a wire which is wound cylindrically at specified intervals, said intervals

being determined such that said shield coils have effects of canceling magnetic field external to said shield coils.

8. (previously amended). The extended Maxwell pair of claim 1 wherein a and d are of the same order of magnitude.

9. (previously amended) The extended Maxwell pair of claim 1 wherein a, b, d and  $z_0$  satisfy an equation given by  $\int_0^{k_{\max}} dk k^4 \{ \sin(kd/2) \sin(kz_0/2)/(kd/2) \} S_0(k) K_0'(ka) I_0(k\rho) = 0$  where  $S_0(k) = 1 - K_1(kb) I_1(ka) / K_1(ka) I_1(kb)$ ,  $I_1$  and  $K_1$  are modified Bessel functions,  $k_{\max}$  is an appropriately selected upper limit of integration and  $\rho$  is an appropriately selected value less than a.

10. (original) The extended Maxwell pair of claim 9 wherein said gradient coils and said shield coils are structured such that said equal currents will have current distribution along said z-axis given by  $j$  and  $j^s$  respectively for said gradient coils and said shield coils, and an shielding equation given by

$$I^s(k) = -(a/b)(I_1(ka)/I_1(kb))I^p(k)$$

is satisfied where  $I_1$  are modified Bessel functions of the first kind,  $I^p(k)$  and  $I^s(k)$  are current density functions  $I^p(z)$  and  $I^s(z)$  respectively for said gradient coils and said shield coils Fourier-transformed into k-space,  $I^p(z) = \int_{-\infty}^{\infty} dz' j^p(\phi, z')$  and  $I^s(z) = \int_{-\infty}^{\infty} dz' j^s(\phi, z')$ .

11. (currently amended) A method of designing an extended Maxwell pair, said extended Maxwell pair comprising:

a pair of cylindrical gradient coil surfaces disposed coaxially around and spaced apart along a z-axis extending in z-direction and symmetrically with respect to an origin, each of said shield coil surfaces being of radius a and of axial length d, said pair being mutually separated by a center-to-center distance  $z_0$  which is greater than d; and

a pair of cylindrical shield coil surfaces disposed coaxially around said primary coils, each of said shield coil surfaces being of radius b which is greater than a;

said method comprising the steps of:

specifying a gradient coil current distribution related to said gradient coils as equal currents are caused to flow through said gradient coils;

obtaining a non-uniform axial shield coil current density distribution related to said shield coils as said equal currents are also caused to flow through said shield coils such that the magnetic field outside said shield coils is cancelled;

expanding resultant magnetic field near said origin due to said equal currents by Fourier-Bessel series;

deriving from said calculated resultant magnetic field a linearity-establishing equation for obtaining a linear gradient around said origin; and

selecting a value of one of the parameters selected from the group consisting of  $d$  and  $z_0$  to solve said linearity-establishing equation for the other of said parameters.

12. (previously amended) The method of claim 11 further comprising the step of approximating said shield coil current distribution by discrete conductor disposition on said cylindrical shield coil .

13. (original) The method of claim 11 wherein said linearity-establishing equation is given by

$$\int_0^{k_{\max}} dk k^4 \{ \sin(kd/2) \sin(kz_0/2)/(kd/2) \} S_0(k) K_0'(ka) I_0(k_p) = 0$$

where  $S_0(k) = 1 - K_1(kb) I_1(ka) / K_1(ka) I_1(kb)$ ,  $I_1$  and  $K_1$  are modified Bessel functions,  $k_{\max}$  is an appropriately selected upper limit of integration and  $\rho$  is an appropriately selected value less than  $a$ .

14. (original) The method of claim 11 wherein said linearity-establishing equation is solved numerically.

15. (original) The method of claim 12 wherein said linearity-establishing equation is solved numerically.

16. (original) The method of claim 13 wherein said linearity-establishing equation is solved numerically.

17. (original) The method of claim 11 further comprising the steps of:

calculating gradient coil current function  $I^p(z) = \int_{-\infty}^z dz' j^p(\varphi, z')$ , where  $j^p(\varphi, z')$  represents said specified gradient coil current distribution;

Fourier-transforming  $I^p(z)$  into k-space to obtain  $I^p(k)$ ;

obtaining a Fourier-transformed shield coil current function  $I^s(k)$  in said k-space by a formula for canceling magnetic field outside said shield coils;

inverse Fourier-transforming  $I^s(z)$  to obtain shield coil current function  $I^s(z)$ ; and

determining positions of loops of a wire to be wound cylindrically to form said shield coils from said shield coil current function  $I^s(z)$ .

18. (original) The method of claim 17 wherein said formula for canceling magnetic field outside said shield coils is given by  $I^s(k) = -(a/b)(I_1(ka)/I_1(kb))I^p(k)$ .

19. (original) The method of claim 11 wherein a and d are of a same order of magnitude.

20. (currently amended) The method of simultaneously achieving a desired RF gradient magnetic field within an inner cylindrical volume of radius a and a field free region outside of an outer coaxial cylindrical volume of radius b, said cylindrical volumes comprising an actively shielded extended Maxwell pair, said actively shielded extended Maxwell pair comprising:

a pair of cylindrical gradient coil surfaces disposed coaxially around and along a z-axis extending in z-direction and symmetrically with respect to an origin, each of said shield coil surfaces being of radius a and of axial length d, said pair being mutually separated by a center-to-center distance  $z_0$  which is greater than d; and further comprising

a pair of cylindrical shield coil surfaces disposed coaxially around said primary coils, each of said shield coil surfaces being of radius b which is greater than a; said method comprising the steps of

specifying a magnetic gradient field distribution in a first cylindrical region of radius a and axial extent inclusive of said center-to-center distance  $z_0$ ,

requiring a null RF magnetic field condition in an annular cylindrical volume

region coextensive with said first cylindrical region, said annular region of external radius b and internal radius a,

deriving a linearity establishing condition from said steps of specifying and requiring, whereby a linear gradient is established in said first cylindrical region,

calculating a gradient coil current distribution to produce the magnetic gradient field distribution of said step (a) of specifying and simultaneously obtaining a shield coil surface current distribution consistent with said step (b) of requiring, said integral of each said current distribution being identical,

approximating said current distributions with axially discrete current loops, and energizing each said approximated current distributions.